# BANGALORE UNIVERSITY 

 Department of MathematicsJnanabharathi Campus
Bengaluru - 560056

Syllabus for
Mathematics Under-Graduate (UG) Programmme

I \& II Semester

Framed according to the National Education Policy (NEP 2020)

September 20, 2021

Proceedings of the BOS meeting in UG-Mathematies-Rogular, hold on $20^{\text {th }}$ September 2021 in the Department of Mathematics, JB Campus, Bangalore University, Bangalore-560 056 at 2.00 pm

The following members attended the meeting to flame the NEP new syllabus for undergraduate degree program B.A./B.Se with mathematics as Major Subject \& B.A./B.Sc.(Hons) Mathematics.

1. Prof. Marina P. Waghmore
2. Prof. Jayadeva. M
3. Prof. T.R. Marulasiddappa
4. Sri. Mahesh H.S
5. Sit. Veena M.G
6. Smt. Shobha. V
7. Dr. Maheshwari P.G
8. Dr. S. Sigarakanti
9. Dr. R. Sumithra


Member Mhualech
Member
Member ushas
Member Malurhisayd
Member

Member


The Chairperson thanked the members for their cooperation.

[Dr. HARINA P. WAGHAMORE]

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## Preamble

The subject wise expert committee to draft model curriculum contents in Mathematics constituted by the Department of Higher Education, Government of Karnataka, Bangalore vide GO No. ED 260 UNE 2019 (PART-1) DATED 13.08.2021 is pleased to submit its partial report on the syllabus for the First Year (First \& Second Semesters) B.Sc.(Basic/Honors) Mathematics and detailed Course Structure for B.Sc.(Honors) Mathematics and M.Sc. (One Year) Mathematics.

The committee discussed various models suggested by the Karnataka State Higher Education Council in its joint meetings with the Chairpersons of Board of Studies of all state universities in Karnataka and resolved to adopt Model IIA (Model Program Structure for the Bachelor of Science (Basic/Hons.) for the subjects with practical's with Mathematics as Major/Minor.

To achieve the core objectives of the National Education Policy 2020 it is unanimously resolved to introduce computer based practical's for the Discipline Core (DSC) courses by using Free and Open Source Software's (FOSS) tools for implementation of theory based on DSC courses as it is also suggested by the LOCF committee that the papers may be taught using various Computer Algebra System (CAS) software's such as Mathematica, MATLAB, Maxima and R to strengthen the conceptual understanding and widen up the horizon of students' selfexperience. In view of these observations the subject expert committee suggested the software's Python/ Maxima/ Scilab/ Maple/ MatLab/ Mathematica for hands on experience of implementation of mathematical concepts in computer based lab.

The expert committee suggests the implementation this curriculum structure in all the Departments of Mathematics in Universities/Colleges in Karnataka.

The subject expert committee designed the Course Learning Outcome (CO) to help the learners to understand the main objectives of studying the courses by keeping in mind of the Programme outcomes (PO) of the graduate degree with honors in Mathematics or a graduate degree with Mathematics as a major subject.

As the Mathematics subject is a vast with several branches of specializations, it is difficult for every student to learn each branch of Mathematics, even though each paper has its own importance. Hence the subject expert committee suggests number of elective papers (for both Discipline electives and Open

Electives) along with Discipline Core Courses. The BoS in Mathematics of universities may include additional electives based on the expertise of their staff and needs of the students'.

A student can select elective paper as per her/his needs and interest. The subject expert committee in Mathematics suggests that the concerned Department/Autonomous Colleges/Universities to encourage their faculty members to include necessary topics in addition to courses suggested by the expert committee.

## B.Sc. Mathematics (Honors)

## Programme Outcomes ( PO ): By the end of the program the students will be able to:

| PO 1 | Disciplinary Knowledge: Bachelor degree in Mathematics is the <br> culmination of in-depth knowledge of Algebra, Calculus, Geometry, <br> differential equations and several other branches of pure and applied <br> mathematics. This also leads to study the related areas such as computer <br> science and other allied subjects. |
| :--- | :--- |
| PO 2 | Communication Skills: Ability to communicate various mathematical <br> concepts effectively using examples and their geometrical visualization. <br> The skills and knowledge gained in this program will lead to the <br> proficiency in analytical reasoning which can be used for modeling <br> and solving of real life problems. |
| PO 3 | Critical thinking and analytical reasoning: The students undergoing <br> this programme acquire ability of critical thinking and logical reasoning <br> and capability of recognizing and distinguishing the various aspects of <br> real life problems. |
| PO 4 | Problem Solving : The Mathematical knowledge gained by the students <br> through this programme develop an ability to analyze the problems, <br> identify and define appropriate computing requirements for its <br> solutions. This programme enhances students overall development and <br> also equip them with mathematical modeling ability, problem solving <br> skills. |
| PO 5 | Research related skills: The completing this programme develop the <br> capability of inquiring about appropriate questions relating to the <br> Mathematical concepts in different areas of Mathematics. |


| PO 6 | Information/digital Literacy: The completion of this programme <br> will enable the learner to use appropriate softwares to solve system <br> of algebraic equation and differential equations. |
| :--- | :--- |
| PO 7 | Self -directed learning: The student completing this program will <br> develop an ability of working independently and to make an in depth <br> study of various notions of Mathematics. |
| PO 8 | Moral and ethical awareness/reasoning: : The student completing this <br> program will develop an ability to identify unethical behavior such as <br> fabrication, falsification or misinterpretation of data and adopting <br> objectives, unbiased and truthful actions in all aspects of life in general <br> and mathematical studies in particular. |
| PO 9 | Lifelong learning: This programme provides self-directed learning and <br> lifelong learning skills. This programme helps the learner to think <br> independently and develop algorithms and computational skills for <br> solving real word problems. |
| PO 10 | Ability to peruse advanced studies and research in pure and applied <br> Mathematical sciences. |

## Assessment

Weightage for the Assessments (in percentage)

| Type of Course | Formative Assessment/ <br> I.A. | Summative Assessment <br> (S.A.) |
| :--- | :---: | :---: |
| Theory | $40 \%$ | $60 \%$ |
| Practical | $50 \%$ | $50 \%$ |
| Projects | $40 \%$ | $60 \%$ |
| Experiential Learning <br> (Internship etc.) | -- | -- |

Contents of Courses for B.Sc. with Mathematics as Major Subject \& B.Sc.(Hons) Mathematics

Model IIA

| $\begin{aligned} & \text { U } \\ & \text { H } \\ & \text { U } \\ & \text { U } \end{aligned}$ | Course No. |  | Uun | Paper Title | Marks |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  |  |  |  |  | S.A. | I.A. |
| I | MATDSCT1.1 | Theory | 4 | Algebra - I and Calculus - I | 60 | 40 |
|  | MATDSCP1.1 | Practical | 2 | Theory based Practical's on Algebra I and Calculus - I | 25 | 25 |
|  | MATOET1.1 | Theory | 3 | (A) Mathematics -I <br> (B) Business Mathematics -I | 60 | 40 |
| II | MATDSCT2.1 | Theory | 4 | Algebra - II and Calculus - II | 60 | 40 |
|  | MATDSCP2.1 | Practical | 2 | Theory based Practical's on Algebra - II and Calculus - II | 25 | 25 |
|  | MATOET2.1 | Theory | 3 | (A) Mathematics -II <br> (B) Business Mathematics-II | 60 | 40 |
| Exit Option with Certificate |  |  |  |  |  |  |
| III | MATDSCT3.1 | Theory | 4 | Ordinary Differential Equations and Real Analysis-I | 60 | 40 |
|  | MATDSCP3.1 | Practical | 2 | Theory based Practical's on Ordinary Differential Equations and Real Analysis-I | 25 | 25 |
|  | MATOET3.1 | Theory | 3 | (A) Ordinary Differential Equations <br> (B) Quantitative Mathematics | 60 | 40 |
| IV | MATDSCT4.1 | Theory | 4 | Partial Differential Equations and Integral Transforms | 60 | 40 |
|  | MATDSCP4.1 | Practical | 2 | Theory based Practical's on Partial Differential Equations and Integral Transforms | 25 | 25 |
|  | MATOET4.1 | Theory | 3 | (A) Partial Differential Equations <br> (B) Mathematical Finance | 60 | 40 |
| Exit Option with Diploma |  |  |  |  |  |  |
| V | MATDSCT5.1 | Theory | 3 | Real Analysis and Complex Analysis | 60 | 40 |
|  | MATDSCP5.1 | Practical | 2 | Theory based Practical's on Real Analysis and Complex Analysis | 25 | 25 |
|  | MATDSCT5.2 | Theory | 3 | Ring Theory | 60 | 40 |
|  | MATDSCP5.2 | Practical | 2 | Theory based Practical's on Ring Theory | 25 | 25 |
|  | MATDSET5.1 | Theory | 3 | (A) Vector Calculus <br> (B) Mechanics <br> (C) Mathematical Logic | 60 | 40 |
| VI | MATDSCT6.1 | Theory | 3 | Linear Algebra | 60 | 40 |
|  | MATDSCP6.1 | Practical | 2 | Theory based Practical's on Linear Algebra | 25 | 25 |


|  | MATDSCT6.2 | Theory | 3 | Numerical Analysis | 60 | 40 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | MATDSCP6.2 | Practical | 2 | Theory based Practical's on Numerical Analysis | 25 | 25 |
|  | MATDSET6.1 | Theory | 3 | (A) Analytical Geometry in3D <br> (B) Number Theory <br> (C) Special Functions <br> (D) History of Bhârtîya Gaṇita | 60 | 40 |
| Exit Option with Bachelor of Arts, B.A./ Bachelor of Science, B.Sc. Degree |  |  |  |  |  |  |
| VII | MATDSCT7.1 | Theory | 3 | Discrete Mathematics | 60 | 40 |
|  | MATDSCP7.1 | Practical | 2 | Theory based Practical's on Discrete Mathematics | 25 | 25 |
|  | MATDSCT7.2 | Theory | 3 | Advanced Ordinary Differential Equations | 60 | 40 |
|  | MATDSCP7.2 | Practical | 2 | Theory based Practical's on Advanced Ordinary Differential <br> Equations | 25 | 25 |
|  | MATDSCT7.3 | Theory | 4 | Advanced Analysis | 60 | 40 |
|  | $\begin{gathered} \hline \text { MATDSET } \\ 7.1 \end{gathered}$ | Theory | 3 | (A) Graph Theory <br> (B) Entire and Meromorphic Functions <br> (C) General Topology <br> (D) Bhâratîya Trikoṇmiti Śâstra | 60 | 40 |
|  | $\begin{gathered} \hline \text { MATDSET } \\ 7.2 \end{gathered}$ | Theory | 3 | Research Methodology in Mathematics | 60 | 40 |
| VIII | MATDSCT8.1 | Theory | 4 | Advanced Complex Analysis | 60 | 40 |
|  | MATDSCT8.2 | Theory | 4 | Advanced Partial Differential Equations | 60 | 40 |
|  | MATDSCT8.3 | Theory | 3 | Fuzzy Sets and Fuzzy Systems | 60 | 40 |
|  | $\begin{gathered} \hline \text { MATDSET } \\ 8.1 \end{gathered}$ | Theory | 3 | (A) Operations Research <br> (B) Lattice theory and Boolean Algebra <br> (C) Mathematical Modeling <br> (D) Aṅkapâśa (Combinatorics) | 60 | 40 |
|  | MATDSET 8.2 | Research Project | $\begin{gathered} 6 \\ (3 \\ + \\ 3) \end{gathered}$ | Research Project* <br> OR <br> Any Two of the following electives <br> (A) Finite Element Methods <br> (B) Cryptography <br> (C) Information Theory and Coding <br> (D) Graph Theory and Networking | $\begin{aligned} & \hline 120 \\ & \text { OR } \\ & 60 \\ & 60 \end{aligned}$ | 80 <br> OR <br> 40 <br> 40 |
| Award of Bachelor of Science Honours, B.Sc.(Hons) Degree in Mathematics |  |  |  |  |  |  |


| One Year M.Sc. degree in Mathematics (Two Semesters) |  |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | Course Number | Theory/ <br> Practic al | Uِ | Title of the Course | S.A. | I.A. |
| I | PGMATDSCT1.1 | Theory | 3 | C++ Programming for Mathematics | 60 | 40 |
|  | PGMATDSCP1.1 | Practical | 2 | Computer Practical's on C++ Programming for Mathematics | 25 | 25 |
|  | PGMATDSCT1.2 | Theory | 3 | Computational Numerical Methods | 60 | 40 |
|  | PGMATDSCP1.2 | Practical | 2 | Computer Practical's on CNM | 25 | 25 |
|  | PGMATDSCT1.3 | Theory | 4 | Functional Analysis | 60 | 40 |
|  | PGMATDSET1.1 | Theory | 3 | (A) Fluid Mechanics -I <br> (B) Computational <br> Fluid Mechanics <br> (C) Contact Geometry <br> (D) Fuzzy Topology <br> (E) Ramanujan Theta Function and Continued Fractions | 60 | 40 |
|  | PGMATDSET1.2 | Theory | 3 | (A) Advanced Graph Theory <br> (B) Partition Theory <br> (C) Algebraic Number Theory <br> (D) Riemannian Geometry | 60 | 40 |
| II | PGMATDSCT2.1 | Theory | 4 | Measure Theory | 60 | 40 |
|  | PGMATDSCT2.2 | Theory | 4 | Differential Geometry | 60 | 40 |
|  | PGMATDSCT2.3 | Theory | 3 | Mathematical Methods | 60 | 40 |
|  | PGMATDSET2.1 | Theory | 3 | (A) Fluid Mechanics -II <br> (B) Magneto hydrodynamics <br> (C) Finsler Geometry and Relativity <br> (D) Mathematical Modeling | 60 | 40 |
|  | PGMATDSET2.2 | Project | 6 | Research Project | 120 | 80 |

- In lieu of the research Project, two additional elective papers/Internship may be offered

Abbreviation for MATDSCT1.1 /MATDSCP1.1
MAT - Mathematics ; DSC - Discipline Core; T - Theory/ P - Practical; 1 - First Semester; . 1 Course 1

PGMATDSCT1.1 : PG- Post Graduate ; MAT- Mathematics; DSC- Discipline Core; TTheory 1 -First Semester; . 1 - Course 1

CURRICULUM STRUCTURE FOR UNDERGRADUATE DEGREE PROGRAM
Name of the Degree Program : B.Sc. (Honors)
Discipline/Subject : Mathematics Starting
Year of Implementation :2021-22
PROGRAM ARTICULATION MATRIX

|  |  | Programme <br> Outcomes that <br> the Course <br> Addresses | Pre-Requisite <br> Course(s) | Pedagogy* | Assessment** |
| :--- | :--- | :--- | :--- | :--- | :--- |
| I |  |  |  |  |  |
| II | MATDSCT1.1 | PO 1, PO 2, PO 3 |  |  |  |

** Pedagogy for student engagement is predominantly Lecture. However, other pedagogies enhancing better student engagement to be recommended for each course. This list includes active learning/ course projects / Problem based or Project based Learning / Case Studies / Self Study like Seminar, Term Paper or MOOC.
${ }^{* * *}$ Every Course needs to include assessment for higher order thinking skills (Applying/ / Evaluating / Creating). However, this column may contain alternate assessment methods that help formative assessment ( i.e. assessment for Learning).

## B.Sc. with Mathematics as a Minor in the $3^{\text {rd }}$ Year

|  | Course No. |  | : | Paper Title | Marks |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  |  |  |  |  | S.A. | I.A. |
| V | MATDSCMT5.1 | Theory | 3 | Complex Analysis | 60 | 40 |
|  | MATDSCMP5.1 | Practical | 2 | Theory based Practical's on Complex Analysis | 25 | 25 |
| VI | MATDSCMT6.1 | Theory | 3 | Numerical Analysis | 60 | 40 |
|  | MATDSCMP6.1 | Practical | 2 | Theory based Practical's on Numerical Analysis | 25 | 25 |

Abbreviation for MATDSCMT5.1 / MATDSCMP5. 1
MAT - Mathematics; DSC - Discipline Core; M - Minor; T - Theory /P - Practical;
5 - Fifth Semester; . 1 - Course 1

Credit Distribution for B.Sc.(Honors) with Mathematics as Major in the $\mathbf{3}^{\text {rd }}$ Year (For Model IIA)

| Subject |  | Major/ Minor in the 3 rdYear | Credits |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  |  |  | Discipline Specific Core (DSC) | Open <br> Elective (OE) | Discipline Specific Elective (DSE) | AECC <br> \&Langu ages | Skill Enhancement Courses (SEC) | Total Credi ts |
| Mathematics | I - IV | Major | $\begin{gathered} 4 \text { Courses } \\ (4+2) \times 4=24 \end{gathered}$ | $\begin{aligned} & 4 \text { Courses } \\ & 3 \times 4=12 \end{aligned}$ | --- | $(4+4=8)$ <br> Courses $\begin{aligned} & 8 x(3+1)= \\ & 32 \end{aligned}$ | $\begin{gathered} 2 \text { Courses } \\ 2 \mathrm{x}(1+1)=4 \end{gathered}$ | 72 |
| Other Subject |  | Minor | 24 | -- | -- | -- | -- | 24 |
|  |  |  |  |  |  |  |  | 96 |
| Mathematics | V \& VI | Major | $\begin{aligned} & 4 \\ & \text { Courses } 4 x(3+2) \\ & =20 \end{aligned}$ | ----- | $\begin{aligned} & 2 \text { Courses } \\ & 2 \times 3=06 \end{aligned}$ | --- | $\begin{gathered} 2 \text { Courses } \\ 2 \times 2=4 \end{gathered}$ | 30 |
| Other Subject |  | Minor | 10 | -- | -- | -- | -- | 10 |
| $(96+40)=\mathbf{1 3 6}$ |  |  |  |  |  |  |  |  |
| Mathematics | $\begin{aligned} & \text { VII \& } \\ & \text { VIII } \end{aligned}$ | Major | $\|$2 Courses <br> $2 \times(3+2)=10$ <br> 3 Courses <br> $3 \times 4=12$ <br> 1 Course <br> $1 \times 3=3$ <br> Total $=25$ | ----- | $\begin{aligned} & 2 \text { Courses } \\ & 2 \times 3=6 \\ & \text { Res.Meth } 1 \\ & \times 3=3 \\ & 2 \text { Courses } \\ & 2 \times 3=6 \\ & \text { Total }=15 \end{aligned}$ | ---- | ----- | 40 |
| Total No. of Courses |  |  | 14 | 04 | 07 | 08 | 04 |  |
| $136+40=176$ |  |  |  |  |  |  |  |  |

# Syllabus for B.Sc. with Mathematics as Major Subject \& 

## B.Sc. (Hons) Mathematics

## SEMESTER - I

| MATDSCT 1.1: Algebra - I and Calculus - I |  |
| :---: | :---: |
| Teaching Hours : 4 Hours/Week | Credits: 4 |
| Total Teaching Hours: 56 Hours | Max. Marks: 100 |
| (S.A.-60 + I.A. - 40) |  |

Course Learning Outcomes: This course will enable the students to

- Learn to solve system of linear equations.
- Solve the system of homogeneous and non homogeneous linear of $m$ equations in $n$ variables by using concept of rank of matrix, finding eigen values and eigenvectors.
- Sketch curves in Cartesian, polar and pedal equations.
- Students will be familiar with the techniques of integration and differentiation of function with real variables.
- Identify and apply the intermediate value theorems and L'Hospital rule.

Unit-I: Matrix: Recapitulation of Symmetric and Skew Symmetric matrices, Algebra of Matrices; Row and column reduction to Echelon form. Rank of a matrix; Inverse of a matrix by elementary operations; Solution of system of linear equations; Criteria for existence of non- trivial solutions of homogeneous system of linear equations. Solution of non-homogeneous system of linear equations. Eigen values and Eigen vectors of square matrices, Cayley-Hamilton theorem, inverse of matrices by Cayley-Hamilton theorem (Without Proof), real symmetric matrices and their properties, reduction of such matrices to diagonal form.

14 Hours
Unit-II: Polar Co-ordinates: Polar coordinates, angle between the radius vector and tangent. Angle of intersection of two curves (polar forms), length of perpendicular from pole to the tangent, pedal equations. Derivative of an arc in Cartesian, parametric and polar forms, curvature of plane curveradius of curvature formula in Cartesian, parametric and polar and pedal forms- center of curvature, asymptotes, evolutes and envelops.

14 Hours
Unit-III: Differential Calculus-I: Limits, Continuity, Differentiability and properties. Properties of continuous functions. Intermediate value theorem, Rolle's Theorem, Lagrange's Mean Value theorem, Cauchy's Mean value theorem and examples. Taylor's theorem, Maclaurin's series, Indeterminate forms and evaluation of limits usingL'Hospitalrule.

14 Hours
Unit-IV: Successive Differentiation: $\mathrm{n}^{\text {th }}$ Derivatives of Standard functions $e^{a x+b},(a x+b)^{n}$, $\log (a x+b), \sin (a x+b), \cos (a x+b), e^{a x} \sin (b x+c), e^{a x} \cos (b x+c)$, Leibnitz theorem and its applications. Tracing of curves (standard curves).

14 Hours

## Reference Books:

1. University Algebra - N.S. Gopala Krishnan, New Age International (P)Limited, 2015.
2. Theory of Matrices - B S Vatsa, New Age International Publishers, 2010.
3. Matrices - A R Vasista, Krishna Prakashana Mandir, 2014.
4. Differential Calculus - Shanti Narayan, S. Chand \& Company, NewDelhi, 1998.
5. Applications of Calculus, Debasish Sengupta, Books and Allied (P) Ltd.,2019.
6. Calculus - Lipman Bers, Holt, Rinehart \&Winston, 1969.
7. Calculus - S Narayanan \& T. K. Manicavachogam Pillay, S. Viswanathan Pvt.Ltd., vol. I \&II, 2009.
8. Schaum's Outline of Calculus - Frank Ayres and Elliott Mendelson, 5th ed. USA: Mc.Graw, 2008.

| MATDSCP 1.1: Practical's on Algebra - I and Calculus - I |  |
| :---: | :---: |
| Practical Hours : 4 Hours/Week | Credits: 2 |
| Total Practical Hours: 56 Hours | Max. Marks: 50 |
| (S.A.-25 + I.A. - 25) |  |

Course Learning Outcomes: This course will enable the students to

- Learn Free and Open Source Software (FOSS) tools for computer programming
- Solve problem on algebra and calculus theory studied in MATDSCT 1.1 by using FOSS software's.
- Acquire knowledge of applications of algebra and calculus through FOSS.


## Practical/Lab Work to be performed in Computer Lab (FOSS)

Suggested Software's: Maxima/Python.

1. Introduction to Python/Maxima.
2. Basic commands in Python/Maxima.
3. Simple examples using Python/Maxima.
4. Matrices -Algebra of matrices.
5. Computation of rank of matrix.
6. Solving the system of homogeneous and non-homogeneous linear algebraic equations.
7. Computation of inverse of matrix using Cayley-Hamilton theorems.
8. Finding the angle between the radius vector and tangent and angle between two curves.
9. Finding the radius of curvature of the given curve.
10. Verification of mean value theorems.
11. Find the Taylor's and Maclaurin's expansion of the given function.
12. Indeterminate forms and evaluation of limits using L-Hospital Rule.
13. Finding the $n^{\text {th }}$ derivative.
14. Tracing of standard curves.

## Open Elective Course

(For students of Science stream who have not chosen Mathematics as one of Core subjects)

| MATOET 1.1: Mathematics - I |  |
| :---: | :---: |
| Teaching Hours : 3 Hours/Week | Credits: 3 |
| Total Teaching Hours: 42 Hours | Max. Marks: 100 |
|  | (S.A.-60 + I.A. - 40) |

Course Learning Outcomes: This course will enable the students to

- Learn to solve system of linear equations.
- Solve the system of homogeneous and non homogeneous $m$ linear equations by using the concept of rank of matrix, finding eigen values and eigenvectors.
- Students will be familiar with the techniques of differentiation of function with real variables.
- Identify and apply the intermediate value theorems and L'Hospital rule.
- Learn to trace some standard curves.

Unit-I: Matrices: Recapitulation of Symmetric and Skew Symmetric matrices, Algebra of Matrices; Row and column reduction, Echelon form. Rank of a matrix; Inverse of a matrix by elementary operations; Solution of system of linear equations; Criteria for existence of non- trivial solutions of homogeneous system of linear equations. Solution of non-homogeneous system of linear equations. Eigen values and Eigen vectors of square matrices, Cayley-Hamilton theorem, inverse of matrices by Cayley-Hamilton theorem (Without Proof). Real symmetric matrices and their properties, reduction of such matrices to diagonal form.

## 14 Hours

Unit-II: Differential Calculus: Limits, Continuity, Differentiability and properties. Intermediate value theorem, Rolle's Theorem, Lagrange's Mean Value theorem, Cauchy's Mean value theorem and examples. Taylor's theorem, Maclaurin's series, Indeterminate forms and examples.

Unit-III: Successive Differentiation: $\mathrm{n}^{\text {th }}$ Derivatives of Standard functions $e^{a x+b},(a x+b)^{n}$, $\log (a x+b), \sin (a x+b), \cos (a x+b), e^{a x} \sin (b x+c), e^{a x} \cos (b x+c)$, Leibnitz theorem and its applications.

14 Hours

## Reference Books:

1. University Algebra - N.S. Gopala Krishnan, New Age International (P)Limited, 2015
2. Theory of Matrices - B S Vatsa, New Age International Publishers, 2010.
3. Matrices - A R Vasista, Krishna Prakashana Mandir, 2014.
4. Differential Calculus - Shanti Narayan, S. Chand \& Company, NewDelhi, 1998.
5. Applications of Calculus, Debasish Sengupta, Books and Allied (P) Ltd.,2019.
6. Calculus - Lipman Bers, Holt, Rinehart \&Winston, 1969.
7. Calculus - S Narayanan \& T. K. Manicavachogam Pillay, S. Viswanathan Pvt. Ltd., vol. I \&II, 2009. 8. Schaum's Outline of Calculus - Frank Ayres and Elliott Mendelson, 5th ed. USA: Mc.Graw, 2008.

# Open Elective <br> (For Students of other than Science Stream) 

| MATOE 1.1(B): Business Mathematics-I |  |
| :---: | :---: |
| Teaching Hours : 3 Hours/Week | Credits: 3 |
| Totat Teaching Hours: 42 Hours | Max. Marks: 100 |
| (S.A.- 60 + I.A. - 40) |  |

Course Learning Outcomes: This course will enable the students to:

- Translate the real word problems through appropriate mathematical modeling.
- Explain the concepts and use equations, formulae and mathematical expression and relationship in a variety of context.
- Finding the extreme values of functions.
- Analyze and demonstrate the mathematical skill require in mathematically intensive areas in economics and business.

Unit-I: Algebra - Set theory and simple applications of Venn Diagram, relations, functions, indices, logarithms, permutations and combinations. Examples on commercial mathematics.

14 Hours
Unit - II: Matrices - Definition of a matrix; types of matrices; algebra of matrices. Properties of determinants; calculations of values of determinants upto third order; Adjoint of a matrix, elementary row and column operations; solution of a system of linear equations having unique solution and involving not more than three variables. Examples on commercial mathematics.

14 Hours
Unit - III: Percentage, Ratios and Proportions - Percentages: Definition, Calculation of percentage, Ratios- Types of Ratios, Duplicate, Triplicate and Sub-Duplicate of ratio, Proportions Definitions and properties- cross product property and Reciprocal property, United proportions Continued proportions - Compound proportions, Examples on commercial mathematics.

14 Hours

## Reference Books:

1. Basic Mathematics, Allen R.G.D, Macmillan, NewDelhi, 1962.
2. Mathematics for Economics, Dowling,E.T., Schaum's Series,McGrawHill,London, 2020.
3. Quantitative Techniques in Management, Vohra, N.D., Tata McGraw Hill, NewDelhi, 2006.
4. Business Mathematics, Soni R.S., Pitamber Publishing House,Delhi, 1996.

## SEMESTER - II

| MATDSCT 2.1: Algebra - II and Calculus - II |  |
| :---: | :---: |
| Teaching Hours : 4 Hours/Week | Credits: 4 |
| Total Teaching Hours: 56 Hours | Max. Marks: 100 |
| (S.A.-60 + I.A. - 40) |  |

Course Learning Outcomes: This course will enable the students to

- Recognize the mathematical objects called Groups.
- Link the fundamental concepts of groups and symmetries of geometrical objects.
- Explain the significance of the notions of Cosets, normal subgroups and factor groups.
- Understand the concept of differentiation and fundamental theorems in differentiation and various rules.
- Find the extreme values of functions of two variables.

Unit-I: Groups-I: Definition of a group with examples and properties, congruence, problems. Subgroups, center of groups, order of an element of a group and its related theorems, cyclic groups, Coset decomposition, Lagrange's theorem and its consequences. Fermat's theorem and Euler's $\phi$ function.

14 hours
Unit-II: Groups-II: Normal subgroups-Examples and problems, Quotient group, Homomorphism and isomorphism of groups, Kernel and Image of a homomorphism, Normality of the kernel, Fundamental theorem of homomorphism, Properties related to isomorphism, Permutation group, Cayley's theorem.

14 hours
Unit-III: Partial Derivatives: Functions of two or more variables-explicit and implicit functions, partial derivatives. Homogeneous functions- Euler's theorem, total derivatives, differentiation of implicit and composite functions, Jacobians and standard properties and illustrative examples. Taylor's and Maclaurin's series for functions of two variables, Maxima- Minima of functions of two variables.

14 hours
Unit-IV: Integral Calculus: Recapitulation of definite integrals and its properties. Line integral: Definition of line integral and basic properties, examples on evaluation of line integrals. Double integral: Definition of Double integrals and its conversion to iterated integrals. Evaluation of double integrals by changing the order of integration and change of variables. Computation of plane surface areas, volume underneath a surface of revolution using double integral. Triple integral: Definition of triple integrals and evaluation-change of variables, volume as triple integral.

14 hours

## Reference Books:

1. Topics in Algebra, I N Herstein, Wiley Eastern Ltd., NewDelhi, 2006.
2. Higher algebra, Bernard \& Child, Arihant, 2016.
3. Modern Algebra, Sharma and Vasista, Krishna Prakashan Mandir, Meerut,U.P,1960.
4. Differential Calculus, Shanti Narayan, S. Chand \& Company, NewDelhi, 1998.
5. Integral Calculus, Shanti Narayan and P K Mittal, S. Chand and Co. Pvt.Ltd., 2015.
6. Schaum's Outline Series, Frank Ayres and Elliott Mendelson, 5th ed. USA: Mc. Graw Hill.,2008.
7. Mathematical Analysis, S C Malik, WileyEastern, 1992.
8. A Course in Abstract Algebra, Vijay K Khanna and S K Bhambri, Vikas Publications, 2018.
9. Text Book of B.Sc. Mathematics, G K Ranganath, S Chand \&Company, 2011.

PRACTICAL

| MATDSCP 2.1: On Algebra -II and Calculus - II |  |
| :--- | :---: |
| Practical Hours : 4 Hours/Week | Credits: 2 |
| Total Practical Hours: 56 Hours | Max. Marks: 50 |
|  | (S.A.-25 + I.A. -25) |

Course Learning Outcomes: This course will enable the students to

- Learn Free and Open Source Software (FOSS) tools for computer programming.
- Solve problem on algebra and calculus by using FOSS software's.
- Acquire knowledge of applications of algebra and calculus through FOSS.


## Practical/Lab Work to be performed in Computer Lab

Suggested Software's: Maxima/Python.

1. Program to construct Cayley's table and test abelian for given finite set.
2. Program to find all possible cosets of the given finite group.
3. Program to find generators and corresponding possible subgroups of a cyclic group.
4. Programs to verification of Lagrange's theorem with suitable examples.
5. Program to verify the Euler's $\phi$ function for a given finite group.
6. Program to verify the given function is Homomorphism and Isomorphism.
7. Program to verify the Euler's theorem and its extension.
8. Program to find Jacobian.
9. Programs to construct series using Maclaurin's expansion for functions of two variables.
10. Program to evaluate the line integrals with constant and variable limits.
11. Program to evaluate the Double integrals with constant and variable limits.
12. Program to evaluate the Triple integrals with constant and variable limits.

## Open Elective

(For students of Science stream who have not chosen Mathematics as one of the Core subjects)

| MATOET 2.1(A): Mathematics - II |  |
| :---: | :---: |
| Teaching Hours : 3 Hours/Week | Credits: 3 |
| Total Teaching Hours: 42 Hours | Max. Marks: 100 |
|  | (S.A.- 60 + I.A. - 40) |

Course Learning Outcomes: This course will enable the students to

- Recognize the mathematical objects called Groups.
- Link the fundamental concepts of groups and symmetries of geometrical objects.
- Explain the significance of the notions of Cosets, normal subgroups and factor groups.
- Understand the concept of differentiation and fundamental theorems in differentiation and various rules.
- Find the extreme values of functions of two variables.
- To understand the concepts of multiple integrals and their applications.

Unit-I: Groups: Definition of a group with examples and properties, congruence, problems. Subgroups, center of groups, order of an element of a group and its related theorems, cyclic groups, Coset decomposition, Factor groups, Lagrange's theorem and its consequences. Fermat's theorem and Euler's $\phi$ function.

14 hours
Unit-II: Partial Derivatives: Functions of two or more variables-explicit and implicit functions, partial derivatives. Homogeneous functions- Euler's theorem, total derivatives, differentiation of implicit and composite functions, Jacobians and standard properties and illustrative examples. Taylor's and Maclaurin's series for functions of two variables, Maxima- Minima of functions of twovariables.

14 hours
Unit-III: Integral Calculus: Recapitulation of definite integrals and its properties. Line integral: Definition of line integral and basic properties, examples on evaluation of line integrals. Double integral: Definition of Double integrals and its conversion to iterated integrals.

14 hours

## Reference Books:

1. Topics in Algebra, I N Herstein, ${ }^{\text {nd }}$ Edition, Wiley Eastern Ltd., NewDelhi, 2006.
2. Higher algebra, Bernard \& Child, Arihant Pub, 2016.
3. Modern Algebra, Sharma and Vasishta, Krishna Prakashan Mandir, Meerut,U.P, 1960.
4. A Course in Abstract Algebra, Vijay K Khanna and S K Bhambri, VikasPublications, 2018.
5. Differential Calculus, Shanti Narayan, S. Chand \& Company, NewDelhi, 1998.
6. Integral Calculus, Shanti Narayan and P K Mittal, S. Chand and Co. Pvt.Ltd., 2015.
7. Schaum's Outline Series, Frank Ayres and Elliott Mendelson, 5th ed. USA:McGraw Hill.,2008.
8. Mathematical Analysis, S.C. Malik, WileyEastern, 1992.
9. Text Book of B.Sc. Mathematics, G.K. Ranganath, S.Chand \& Company, 2011.

## Open Elective

## (For Students of other than science stream)

| MATOET 2.1(B): Business Mathematics-II |  |
| :---: | :---: |
| Teaching Hours : 3 Hours/Week | Credits: 3 |
| Total Teaching Hours: 42 Hours | Max. Marks: 100 |
|  | (S.A.- 60 + I.A. -40) |

Course Learning Outcomes: This course will enable the students to

- Integrate concept in international business concept with functioning of global trade.
- Evaluate the legal, social and economic environment of business.
- Apply decision-support tools to business decision making.
- Will be able to apply knowledge of business concepts and functions in an integrated manner.

Unit - I: Mathematical logic: Propositions, Truth values, Logical connectives, Truth table, Tautology and Contradiction, Logical equivalence, Negations, Converse, Inverse and Contrapositive of condition proposition and examples on commercial mathematics.

14 hours
Unit - II: Commercial Arithmetic: Interest: Concept of Present value and Future value, Simple interest, Compound interest, Nominal and Effective rate of interest, Examples and Problems Annuity: Ordinary Annuity, Sinking Fund, Annuity due, Present Value and Future Value of Annuity, Equated Monthly Installments (EMI) by Interest of Reducing Balance and Flat Interest methods, Examples and Problems.

14 Hours
Unit - III: Measures of central Tendency and Dispersion: Frequency distribution: Raw data, attributes and variables, Classification of data, frequency distribution, cumulative frequency distribution, Histogram and give curves. Requisites of ideal measures of central tendency, Arithmetic Mean, Median and Mode for ungrouped and grouped data. Combined mean, Merits and demerits of measures of central tendency, Geometric mean: definition, merits and demerits, Harmonic mean: definition, merits and demerits, Choice of A.M., G.M. and H.M. Concept of dispersion, Measures of dispersion: Range, Variance, Standard deviation (SD) for grouped and ungrouped data, combined SD, Measures of relative dispersion: Coefficient of range, coefficient of variation. Examples and problems.

14 Hours

## Reference Books:

1. Practical Business Mathematics, S. A. Bari New Literature Publishing Company New Delhi, 1971.
2. Mathematics for Commerce, K. Selvakumar Notion Press Chennai, 2014.
3. Business Mathematics with Applications, Dinesh Khattar\& S. R. Arora S. Chand Publishing New Delhi, 2001.
4. Business Mathematics and Statistics, N.G. Das \&Dr. J.K. Das McGraw Hill New Delhi, 2017. 5. Fundamentals of Business Mathematics, M. K. Bhowal, Asian Books Pvt. Ltd New Delhi, 2007. 6. Mathematics for Economics and Finance: Methods and Modeling, Martin Anthony and Norman, Biggs Cambridge University Press Cambridge, 2009.
5. Financial Mathematics and its Applications, Ahmed Nazri Wahidudin Ventus Publishing APS Denmark, 2011.
6. Fundamentals of Mathematical Statistics, Gupta S.C. and Kapoor V.K, Sultan Chand and Sons, New Delhi, 2002.
7. Statistical Methods, Gupta S.P.: Sultan Chand and Sons, New Delhi, 2021.
8. Applied Statistics, Mukhopadhya Parimal New Central Book Agency Pvt. Ltd. Calcutta, 2018.
9. Fundamentals of Statistics, Goon A.M., Gupta M.K. and Dasgupta, B. World Press Calcutta, 2008.
10. Fundamentals of Applied Statistics, , Gupta S.C. and Kapoor V.K, Sultan Chand and Sons, New Delhi, 2014.
