## IV Semester B.A./B.Sc. Examination, September/October 2022 (Semester Scheme) (CBCS) (F+R) (2015 – 16 and Onwards) MATHEMATICS (Paper – IV)

Time: 3 Hours

Max. Marks: 70

 $(5 \times 2 = 10)$ 

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Instruction: Answer all Parts.

PART - A

- 1. Answer any five questions:
  - a) Define homomorphism and isomorphism of a group.
  - b) Define centre of a group.
  - c) Write the formula for b<sub>n</sub> of Fourier sine series expansion.
  - d) Find the critical points of the function  $f(x, y) = 2x^2 xy + y^2 + 7x$ .
  - e) Find  $L^{-1} \left\{ \frac{5s}{s^2 + 9} \right\}$ .
  - f) Find L{e3t sin5t}.
  - g) Solve  $\frac{d^2y}{dx^2} 6\frac{dy}{dx} + 8y = 0$ .
  - h) Find the complementary function of  $(D^2 4)y = 0$ .

PART - B

Answer any one full question :

 $(1 \times 15 = 15)$ 

- 2. a) Show that a subgroup H of a group G is normal subgroup iff  $gHg^{-1} = H$ ,  $\forall g \in G$ .
  - b) Let f: G → G' be a homomorphism from the group G into G' with Kernel K, then show that f is one-one if and only if K = {e} where e is the identity element of G.
  - c) Prove that the centre of a group G is normal subgroup of G.

OR

P.T.O.