NS – 607

I Semester B.C.A. Degree Examination, November/December 2016
(CBCS) (F+R)
(2014-15 & Onwards)
BCA – 105 : DISCRETE MATHEMATICS

Time : 3 Hours

Max. Marks : 100

Instruction *: Answer* ***all*** *Sections.*

SECTION – A

I. Answer **any ten** : **(10×2=20)**

1) If A = {x|x∈N and x<3 } and B = {0, 1, 3}. Find A – B.

2) If A = {1, 2, 3}, B = {3, 4, 5} and C = { 0, 2, 3}, find (A∩B)×C.

3) Construct truth table for the proposition p ∨ ~q.

4) Find x, y, z if $\begin{bmatrix} 4-y & 3 \\ x & 5 \end{bmatrix} = \begin{bmatrix} -1 & z+1 \\ 1 & 5 \end{bmatrix}$.

5) If $A = \begin{bmatrix} 1 & -2 \\ -1 & 0 \end{bmatrix}$ and $B = \begin{bmatrix} 2 & 0 & 3 \\ 3 & 1 & 4 \end{bmatrix}$, find AB.

6) Find the characteristic equation of the matrix $\begin{bmatrix} 1 & -2 \\ 3 & 0 \end{bmatrix}$.

7) Prove that $\log_b a . \log_c b . \log_a c = 1$.

8) Find n if $2\,({}^nP_3) = {}^nP_5$.

9) On the set of integers Z, the binary operation * is defined by $a*b = \frac{ab}{3}, \forall a, b \in Z$. Find identity element.

10) If $\vec{a} = 2\hat{i} - 3\hat{j} + 4\hat{k}, \vec{b} = \hat{i} - \hat{j} + 2\hat{k}$ find unit vector along $\vec{a} - \vec{b}$.

P.T.O.

11) Find the midpoint of line joining (–2, 8) and (1, – 2).

12) Find the equation of the line passing through (–1, 2) and having slope 3.

SECTION – B

II. Answer **any six** of the following : **(6×5 =30)**

13) If A = {1, 4}, B = {2, 3, 6}, C = {2, 3, 7} then verify that A×(B – C) = (A×B) – (A×C).

14) Show that the function f : R $\rightarrow$ R defined by f(x) = 4x + 3 is invertible. Find the inverse of f.

15) Show that $p \vee (q \wedge r) \leftrightarrow [(p \vee q) \wedge (p \vee r)]$ is a tautology.

16) If $(p \rightarrow q) \wedge (p \wedge r)$ is given to be false, find the truth values of p, q, r.

17) Write the truth table of $(p \vee q) \vee \sim p$. Show that the compound propositions $p \wedge q$ and $\sim (p \rightarrow \sim q)$ are logically equivalent.

18) Find the inverse of the matrix $A = \begin{bmatrix} 3 & -3 & 4 \\ 2 & -3 & 4 \\ 0 & -1 & 1 \end{bmatrix}$.

19) Using Cramer's rule solve 3x – y + 2z =13 ; 2x + y – z = 3; x + 3y –5z = – 8.

20) Verify Cayley Hamilton theorem for the matrix $\begin{bmatrix} 1 & 4 \\ -2 & 3 \end{bmatrix}$.

SECTION – C

III. Answer **any six** of the following. **(6×5 =30)**

21) If $\log\left(\frac{a-b}{5}\right) = \frac{1}{2}(\log a + \log b)$, show that $a^2 + b^2 = 27\,ab$.

22) Find the number of three digit even numbers that can be formed using 2, 3, 4, 5, 6 repetitions being not allowed.

23) If ${}^{n+2}C_8 : {}^{n-2}P_4 = 57 : 16$ find n.

24) Prove that the set G = { 3n | n∈Z} is an abelian group w.r.t. addition.

25) Prove that the set G = {2, 4, 6, 8} is an abelian group w.r.t. multiplication modulo 10.

26) If $\vec{a} = \hat{i} - \hat{j} + 2\hat{k}$, $\vec{b} = 2\hat{i} + 3\hat{j} - \hat{k}$ find $(\vec{a} + 2\vec{b}).(2\vec{a} - \vec{b})$.

27) Show that the points A(1,2,3), B (2, 3, 1) and C (3,1,2) are vertices of an equilateral triangle.

28) If the vectors $4\hat{i} + 11\hat{j} + m\hat{k}$, $7\hat{i} + 2\hat{j} + 6\hat{k}$ and $\hat{i} + 5\hat{j} + 4\hat{k}$ are coplanar, then find 'm'.

SECTION – D

IV. Answer **any four** of the following. **(4×5 =20)**

29) Prove that the points (6, 4), (7, – 2), (5, 1), (4, 7) form vertices of a parallelogram.

30) The three vertices of a parallelogram taken in order are (8,5), (–7, –5) and (– 5, 5). Find the co-ordinate of the fourth vertex.

31) Find the equation of the locus of a point which moves such that its distance from X-axis is twice its distance from Y-axis.

32) Derive the equation of the straight line whose x -intercept is 'a' and y-intercept is 'b'.

33) Find 'K' for which the lines 2x – ky + 1 = 0 and x + (k+1) y –1 = 0 are perpendicular.

34) Find the equation of straight line which is passing through intersection of the lines 2x – 3y – 4 = 0 and 2x + 2y – 1 = 0 and perpendicular to the line x + 4y – 8 = 0.